

# **SOLUTIONS**

## **PROGRESS TEST-2**

**RB-1815**

**RBS-1803-1804**

**JEE ADVANCED PATTERN**

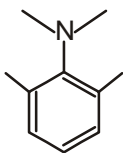
**Test Date: 15-10-2017**



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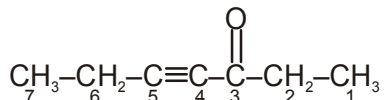
## CHEMISTRY

1. (C)



Due to steric hinderence molecule become non planar. So no resonance possible.

2. (C)



3. (D)

Larger number of bond and minimum charge separation make structure most stable.

4. (B)

Let x mole  $\text{NH}_3$  is evolved

Now, total g eq. of acid = total g eq. of base

$$1 \times 1 \times 1 = x \times 1 + 1 \times \frac{1}{7} \text{N}$$

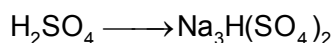
$$\text{or, } x = \frac{6}{7}$$

$$\text{Also, mole of N} = \frac{6}{7} \times 1 = \frac{6}{7}$$

$$\text{mass of N} = \frac{6}{7} \times 14 = 12 \text{ g}$$

$$\% \text{ of N in the compound} = \frac{12}{50} \times 100 = 24$$

5. (D)



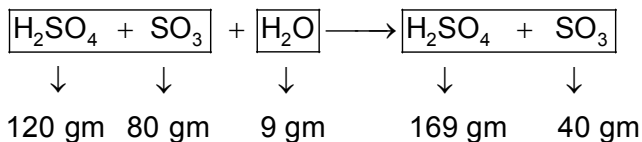
$$\text{n.f.} = \left[ 2 - \frac{1}{2} \right] = \frac{3}{2}$$

$$\text{Equivalent mass} = \frac{98}{3/2} = \frac{2}{3} \times 98 = 65.33$$

6. (B)

200 gm (109%)

New oleum

**New oleum**

∴ 209 gm new oleum can give maximum of 218 gm H<sub>2</sub>SO<sub>4</sub>.

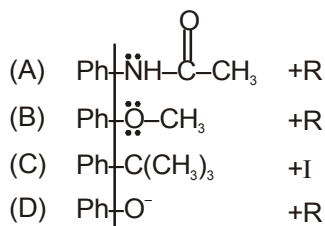
∴ 100 gm new oleum can give maximum of  $\frac{218}{209} \times 100 = 104.30$

∴ % labelling of new oleum = 104.3%

7. (A)

8. (A)

9. (A,B,D)



10. (A,C)

m.g. eq of I<sup>-</sup> = 10;      m.g. eq of IO<sub>3</sub><sup>-</sup> = 50

So, I<sup>-</sup> is limiting

n-factor of I<sub>2</sub> = 5/3

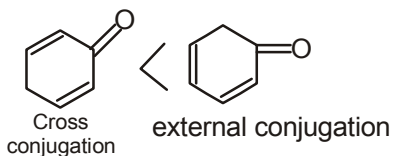
So, m.mole of I<sub>2</sub> =  $\frac{10}{\frac{5}{3}} = 6$

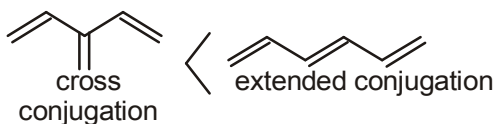
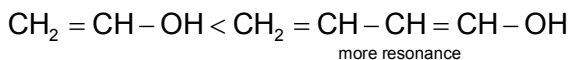
m.mole of MnO<sub>4</sub><sup>-</sup> =  $\frac{6 \times 14}{5} = 16.8$

m.mole of Mn<sup>+2</sup> = 16.8

11. (B,C,D)

so, Ph-CH<sub>2</sub>-Ph > Ph-CH=CH<sub>2</sub>





12. (B,C,D)

13. (A, B, C)

$$M_{\text{mix}} = \frac{M_1 V_1 + M_2 V_2 + M_3 V_3}{V_1 + V_2 + V_3}$$

$$\text{For } 1 : 1 : 5 \Rightarrow M_{\text{mix}} = \frac{12 + 6 + 10}{7} = \frac{28}{7} = 4 \text{ M}$$

$$\text{For } 1 : 2 : 6 \Rightarrow M_{\text{mix}} = \frac{12 + 12 + 12}{9} = \frac{36}{9} = 4 \text{ M}$$

$$\text{For } 1 : 3 : 7 \Rightarrow M_{\text{mix}} = \frac{12 + 18 + 14}{11} = \frac{44}{11} = 4 \text{ M}$$

$$\text{For } 1 : 2 : 5 \Rightarrow M_{\text{mix}} = \frac{12 + 12 + 10}{8} = \frac{34}{8} \neq 4 \text{ M}$$

14. (A)

15. (B)

16. (A)

17. (D)

18. (C)

19. (4)

$\frac{100}{29}$  (M) NaOH (aq.) solution, means,

$\frac{100}{29}$  moles of NaOH is present in 1000g solution.

$$\text{So, mass of solvent} = \left( 1000 - \frac{100}{29} \times 40 \right) \text{g} = \frac{25000}{29} \text{g} = \frac{25}{29} \text{kg}$$

$$\text{So, molality} = \frac{100}{29 \times \frac{25}{29}} = 4 \text{ m}$$

20. (5)

Let x moles of  $\text{Cl}_2$  is liberated from bleaching powder then,  
 gram equivalent of  $\text{Cl}_2 = \text{gram equivalent of I}_2 = \text{gram equivalent of Na}_2\text{S}_2\text{O}_3$ .

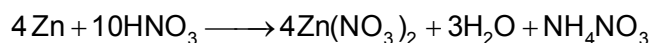
$$\text{or, } x \times 2 = 2 \times \frac{1}{10} \times 1$$

$$\text{or, } x = 0.1$$

$$\text{i.e., mass of Cl}_2 \text{ liberated} = 0.1 \times 71 \text{ g}$$

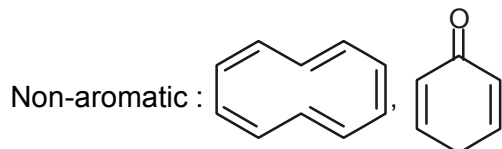
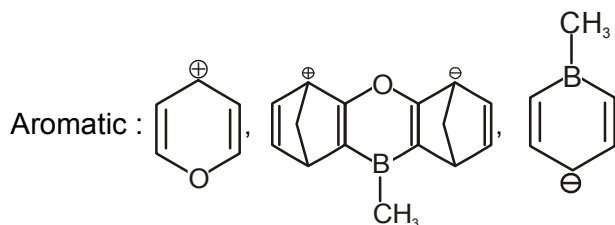
$$\text{So, \% of available chlorine} = \frac{7.1}{142} \times 100 = 5\%$$

21. (8)



$$a = 4; b = 3; c = 1 \Rightarrow a + b + c = 4 + 3 + 1 = 8$$

22. (5)

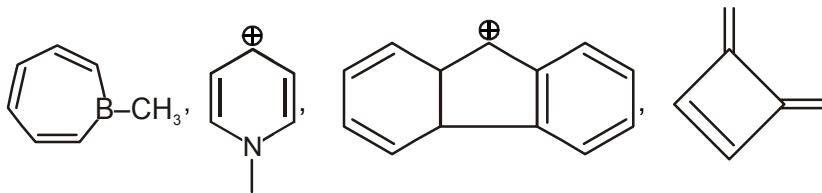


Remaining four structures are anti-aromatic.

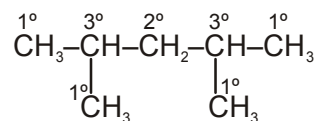
23. (6)

24. (4)

Six electrons delocalised structures are :



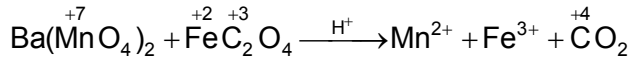
25. (4)



26. (5)

27. (6)

28. (2)



$$\text{n.f.} = 10 \quad \text{n.f.} = (1 + 2 = 3)$$

$$\text{g eq. Ba}(\text{MnO}_4)_2 = \text{g eq. FeC}_2\text{O}_4$$

$$\Rightarrow (1) \left( \frac{1}{10} \times 10 \right) = \left( \frac{1}{6} \right) (x \times 3) = \frac{x}{2} \Rightarrow x = 2$$

## MATHEMATICS

29. (D)

$$\frac{a}{\sqrt{cb}} - 2 = \sqrt{\frac{b}{c}} + \sqrt{\frac{c}{b}} \Rightarrow a = b + c + 2\sqrt{bc} \Rightarrow a = (\sqrt{b} + \sqrt{c})^2$$

$$\Rightarrow (\sqrt{a} - \sqrt{b} - \sqrt{c})(\sqrt{a} + \sqrt{b} + \sqrt{c}) = 0 \Rightarrow \sqrt{a} + \sqrt{b} + \sqrt{c} = 0 \text{ (not valid)}$$

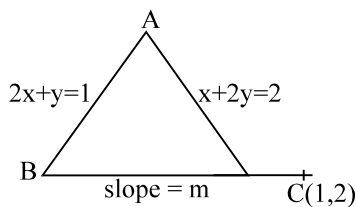
$$-\sqrt{a} + \sqrt{b} + \sqrt{c} = 0$$

$$\text{hence } x = -1, y = 1$$

30. (B)

$$\text{Slope of AB} = -2; \text{ slope of AC} = \frac{-1}{2}; \text{ slope of BC} = m$$

$$\frac{m+2}{1-2m} = \frac{-\frac{1}{2}-m}{1-\frac{1}{2}m} \Rightarrow 4 - m^2 = -(1 - 4m^2) = 4m^2 - 1$$



$$5m^2 = 5 \quad \Rightarrow \quad m = \pm 1$$

$$(y - 2) = 1(x - 1) \quad \text{or} \quad (y - 2) = -1(x - 1)$$

$$\text{x-intercept } x = -1 \quad x = 3 \text{ Ans.}$$

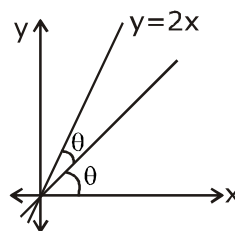
31. (B)

$$\tan 2\theta = 2$$

$$\therefore \frac{2 \tan \theta}{1 - \tan^2 \theta} = 2$$

$$\Rightarrow \tan^2 \theta + \tan \theta - 1 = 0$$

$$\therefore \tan \theta = \frac{\sqrt{5} - 1}{2} \text{ Ans.}$$



32. (A)

$$\text{Circumcentre } O \equiv \left(-\frac{1}{3}, \frac{2}{3}\right) \text{ and orthocentre } H \equiv \left(\frac{11}{3}, \frac{4}{3}\right)$$

$$\therefore \text{coordinate of } G \text{ are } \left(1, \frac{8}{9}\right)$$

$$A(1, 10), G \left(1, \frac{8}{9}\right)$$

$$AG : GD = 2 : 1$$

$$\therefore D = \left(1, -\frac{11}{3}\right)$$

$$\therefore \text{coordinate of the mid point of } BC \text{ are } \left(1, -\frac{11}{3}\right)$$

33. (B)

$$\frac{2-x-x^2}{1+x^2} \geq 1$$

$$\Rightarrow 2x^2 + x - 1 \leq 0 \Rightarrow (2x-1)(x+1) \leq 0$$

$$\Rightarrow x \in \left[-1, \frac{1}{2}\right]$$

34. (C)

35. (D)

$$\begin{aligned} t_1 &= \frac{1}{\sin \theta \cdot \sin 3\theta} = \frac{\sin 2\theta}{\sin \theta \cdot \sin 2\theta \cdot \sin 3\theta} = \frac{\sin(3\theta - \theta)}{\sin \theta \cdot \sin 2\theta \cdot \sin 3\theta} \\ &= \frac{1}{\sin 2\theta} \cdot \left[ \frac{\sin 3\theta \cdot \cos \theta - \cos 3\theta \cdot \sin \theta}{\sin \theta \cdot \sin 3\theta} \right] = \frac{1}{\sin 2\theta} [\cot \theta - \cot 3\theta] \end{aligned}$$

$$t_2 = \frac{1}{\sin 2\theta} [\cot 3\theta - \cot 5\theta]$$

$$t_3 = \frac{1}{\sin 2\theta} [\cot 5\theta - \cot 7\theta]$$

$$\vdots$$

$$t_{20} = \frac{1}{\sin 2\theta} [\cot 39\theta - \cot 41\theta]$$

Summing, we get

$$\therefore S_{20} = \frac{1}{\sin 2\theta} [\cot \theta - \cot 41\theta]$$

36. (C)

$$y = \frac{\{\sin x\}}{1 + \{\sin x\}}$$

$$\{\sin x\} = \frac{1}{1-y} - 1 \quad \because 0 \leq \{\sin x\} < 1$$

$$\therefore 0 \leq \frac{1}{1-y} - 1 < 1 \Rightarrow y \in [0, 1/2)$$

37. (A, C, D)

38. (A, C, D)

$$P(x) = \frac{1-x^{18}}{1+x}$$

$$= \frac{1-(y-1)^{18}}{y} = \frac{1-(1-y)^{18}}{y}$$

coefficient of  $y^2$  in  $\left\{ \frac{1-(1-y)^{18}}{y} \right\}$  is coefficient of  $y^3$  in  $(1-y)^{18} = {}^{18}C_3 = 816$

39. (A, B)

$f(g(x))$  is even, periodic, unbounded & positive  $\forall x$  in domain.



40. (A, C)

$$4^x - 2^{x+2} + 5 + ||b-1|-3| = |\sin y|$$

$$= 4^x - 2^x \cdot 4 + 4 + 1 + ||b-1|-3| = |\sin y|$$

$$\Rightarrow (2^x - 2)^2 + 1 + ||b-1|-3| = |\sin y|$$

Now, LHS  $\geq 1$  and RHS  $\leq 1$ , equality is possible only when LHS = RHS = 1.

$$\therefore ||b-1|-3| = 0$$

$$\Rightarrow |b-1| = 3 \Rightarrow b-1 = \pm 3$$

$$\therefore b = 4, -2$$

41. (B, D)

Dividing by  $\cos(2012^\circ)$ , we get

$$\tan \theta = \frac{1 + \tan 2012^\circ}{1 - \tan 2012^\circ}$$

$$\Rightarrow \tan \theta = \tan(2012^\circ + 45^\circ) = \tan 2057^\circ$$

$$\Rightarrow \text{Hence } \theta = k(180^\circ) + 2057^\circ$$

Put  $k = -10$

$$\theta = 2057^\circ - 1800^\circ = 257^\circ$$

$$\text{If } k = -11 \Rightarrow \theta = 77^\circ$$

42. (A)

$$A = -\log_2 \left( \frac{1}{2} - x \right) + \log_2 \sqrt{(2x-1)^2}$$

$$A = \log_2 \frac{|2x-1|}{\left( \frac{1-2x}{2} \right)} = \log_2 2 = 1$$

$$B^2 = 10 - 1 \Rightarrow B = \pm 3$$

43. (C)

$$\log_3(c^3 - 18) = 2 \Rightarrow c = 3$$

44. (A)

45. (B)

Image of A(1, 3) in line  $x + y = 2$  is

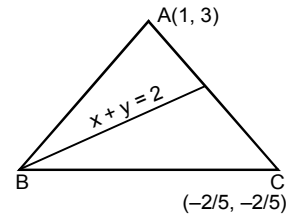
$$\left(1 - \frac{2(2)}{2}, 3 - \frac{2(2)}{2}\right) = (-1, 1)$$

So line BC passes through  $(-1, 1)$  and  $\left(-\frac{2}{5}, -\frac{2}{5}\right)$ .

$$\text{Equation of line BC is } y - 1 = \frac{-2/5 - 1}{-2/5 + 1}(x + 1)$$

$$\Rightarrow y - 1 = \frac{-7}{3}(x + 1) \Rightarrow 3y - 3 = -7x - 7$$

$$\Rightarrow 7x + 3y + 4 = 0$$

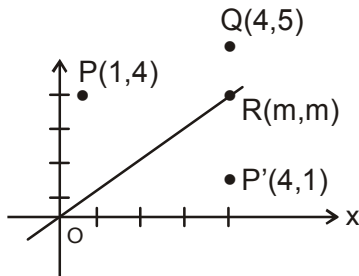


46. (C)

Vertex B is point of intersection of

$$7x + 3y + 4 = 0 \text{ and } x + y = 2$$

47. (4)

Image of  $(1, 4)$  about the line  $y = x$  is  $(4, 1) \Rightarrow P'(4, 1)$   $Q(4, 5)$  and  $R(m, m)$  are collinear.

$$\Rightarrow m = 4$$

48. (0)

minimum value of R.H.S. = 2, at  $x=1$  and maximum value of L.H.S. is 2 at  $x = 2n\pi, n \in \mathbb{I}$ 

Thus no. of real solution = 0.

49. (5)

Differentiate w.r.t.  $\theta$  and put  $\theta = \frac{\pi}{2}$ .

50. (0)

$$\sin x = \cos^2 x$$

$$\begin{aligned} \text{Also } \cos^{12}x + 3\cos^{10}x + 3\cos^8x + \cos^6x - 1 &= (\cos^4x + \cos^2x)^3 - 1 \\ &= (\sin^2x + \sin x)^3 - 1 = 0 \end{aligned}$$

51. (1)

$$a = \log_{12} 18 \text{ \& } b = \log_{24} 54$$

$$a = \frac{\log_2 18}{\log_2 12} = \left( \frac{2\log_2 3 + 1}{\log_2 3 + 2} \right), \quad b = \frac{\log_2 54}{\log_2 24} = \left( \frac{3\log_2 3 + 1}{\log_2 3 + 3} \right)$$

$$\text{Let } \log_2 3 = x \Rightarrow a = \left( \frac{2x+1}{x+2} \right) \quad b = \left( \frac{3x+1}{x+3} \right)$$

$$ab + 5(a - b) = \frac{(2x+1)(3x+1)}{(x+2)(x+3)} + 5 \left( \frac{2x+1}{x+2} - \frac{3x+1}{x+3} \right)$$

$$= \frac{6x^2 + 5x + 1 + 5(2x^2 + 7x + 3 - 3x^2 - 7x - 2)}{(x+2)(x+3)}$$

$$= \frac{x^2 + 5x + 6}{(x+2)(x+3)} = \frac{(x+2)(x+3)}{(x+2)(x+3)} = 1$$

52. (5)

$$3x - 7 \leq x^2 - 3x + 2 < 3x - 7 + 1 \quad \& \quad 3x \in \mathbb{Z}$$

$$\Rightarrow 0 \leq x^2 - 6x + 9 < 1 \quad \& \quad 3x \in \mathbb{Z}$$

$$\Rightarrow 2 < x < 4 \quad \& \quad 3x = n \text{ for some } n \in \mathbb{Z}$$

$$\Rightarrow 2 < \frac{n}{3} < 4 \quad \& \quad x = \frac{n}{3}, n \in \mathbb{Z} \qquad \Rightarrow 6 < n < 12 \quad \& \quad x = \frac{n}{3}, n \in \mathbb{Z}$$

$$\Rightarrow n \in \{7, 8, 9, 10, 11\} \quad \& \quad x = \frac{n}{3}, n \in \mathbb{Z} \qquad \Rightarrow x \in \left\{ \frac{7}{3}, \frac{8}{3}, 3, \frac{10}{3}, \frac{11}{3} \right\}$$

53. (4)

The period of the function is 8

$$\therefore \sum_{r=0}^{\infty} (f(1+8r))^r = 5$$

$$\Rightarrow 1 + f(1) + (f(1))^2 + \dots \infty \text{ terms} = 5$$

$$\frac{1}{1-f(1)} = 5$$

$$5f(1) = 4$$

54. (2)

$[\cot^{-1} x] + 2[\tan^{-1} x] = 0$ , will be satisfied only when

$$[\cot^{-1} x] = 0 \text{ \& \ } [\tan^{-1} x] = 0$$

or  $[\cot^{-1} x] = 2 \text{ \& \ } [\tan^{-1} x] = -1$

**Case-I**  $[\cot^{-1} x] = 0 \Rightarrow x \in (\cot 1, \infty)$

$\& [\tan^{-1} x] = 0 \Rightarrow x \in [0, \tan 1)$

$\therefore x \in (\cot 1, \tan 1)$

**Case-II**  $[\cot^{-1} x] = 2 \Rightarrow x \in (\cot 3, \cot 2]$

$\& [\tan^{-1} x] = -1 \Rightarrow x \in [-\tan 1, 0)$

$\therefore x \in [-\tan 1, \cot 2]$

Thus the solution set for the given equation is

$$[-\tan 1, \cot 2] \cup (\cot 1, \tan 1) \Rightarrow x = 1, -1$$

55. (7)

Let  $x = l + f$                        $0 \leq f < 1$

$$73l + \left[ f + \frac{1}{19} \right] + \left[ f + \frac{1}{20} \right] + \dots + \left[ f + \frac{1}{91} \right] = 546$$

Now  $546 = 7 \times 73 + 35$

$\Rightarrow l = 7$

56. (5)

Put  $\theta = 0$ , then  $2^7 = 1 + a + b + c + d$

$\Rightarrow a + b + c + d = 127$

$\therefore (a + b + c + d - 2)^{\frac{1}{3}} = (125)^{\frac{1}{3}} = 5$

## PHYSICS

57. (A)

Force is parallel to a line  $y = \frac{3}{2}x + c$

The equation of given line can be written as

$$y = -\frac{k}{3}x + \frac{5}{3}$$

Work done will be zero, when force is perpendicular to the displacement i.e., the above two lines are perpendicular or

$$m_1 m_2 = -1$$

$$\text{or } \left(\frac{3}{2}\right) \left(-\frac{k}{3}\right) = -1$$

$$\text{or } k = 2$$

58. (C)

$$= r(\sqrt{2} + 1)$$

59. (B)

$$f = \mu(m_1 + m_2 + m_3)g = 0.4(3 + 2 + 1) \times 10 = 24 \text{ N}$$

$$\text{To move the blocks } F \geq f, \quad 3t \geq 24, \quad t \geq 8 \text{ s}$$

60. (C)

Friction between  $P$  and  $Q$  will retard  $P$  (and accelerate  $Q$ ) till slipping is stopped

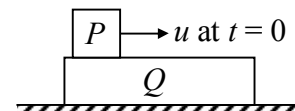
Masses of the blocks are same so

$\therefore$  Retardation of  $P$  = acceleration of  $Q$  =  $\mu g$

$$\text{Thus } v_p = u - \mu g t \quad \text{and } v_q = \mu g t$$

Once slipping is stopped both blocks will move with same velocity

(i.e.  $\frac{u}{2}$ ). Graph (C) depicts this treatment.



61. (A)

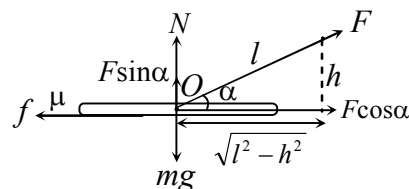
$$N = mg - F \sin \alpha$$

$$F \cos \alpha = f = \mu N$$

$$F \cos \alpha = \mu(mg - F \sin \alpha)$$

$$\mu = \frac{F \cos \alpha}{mg - F \sin \alpha} = \frac{F \times \frac{\sqrt{l^2 - h^2}}{l}}{mg - F \times \frac{h}{l}}$$

$$\mu = \frac{F \sqrt{l^2 - h^2}}{mgl - Fh}$$



62. (C)

$$-\frac{1}{nu} - \frac{1}{u} = \frac{-1}{f}, \quad u = \left(\frac{n+1}{n}\right)f$$

63. (C)

The maximum velocity of the insect is  $A\sqrt{\frac{k}{M}}$ .

Its component perpendicular to the mirror is  $A\sqrt{\frac{k}{M}} \sin 60^\circ$ .

Thus maximum relative speed =  $\sqrt{3}A\sqrt{\frac{k}{M}}$ .

64. (A)

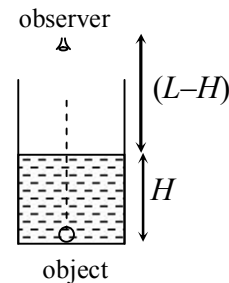
$$X_{app} = L - H + \frac{H}{\mu}$$

$$\frac{dX_{app}}{dt} = \frac{dH}{dt} \left( \frac{1-\mu}{\mu} \right)$$

$$\pi r^2 H = V$$

$$\therefore \frac{dH}{dt} = -\frac{2H}{r} \frac{dr}{dt} = \frac{2KH}{r}$$

$$\therefore \frac{dX_{app}}{dt} = \frac{2KV}{\pi r^3} \left( \frac{1-\mu}{\mu} \right)$$



65. (A) (B) and (C)

$$\text{Here } 10 - T_2 = 10a \quad \dots (i)$$

$$T_2 - T_1 - 0.3 \times 2g = 3a \quad \dots (ii)$$

$$T_1 - 0.3 \times 2g = 2a$$

$$\text{Summing up } 10g - 0.3 \times 4 \times g = 15a$$

$$\text{i.e. } a = 5.86 \text{ ms}^{-2}$$

$$T_2 = 10 \times 9.8 - 10 \times 5.86 \text{ ms}^{-2} = 41.4 \text{ N}$$

$$T_1 = 2 \times 5.86 + 0.6 \times 9.8 = 17.7 \text{ N}$$

**66. (B) and (D)**

From FBD of A with respect to B

$$a_v = 0$$

$$mg = N - ma \sin \theta$$

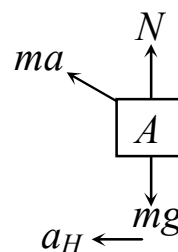
$$\Rightarrow N = mg - ma \sin \theta$$

$$ma \cos \theta = ma_H \Rightarrow a_H = a \cos \theta$$

If block B is having friction then, for  $a_H = 0$

$$ma \cos \theta \leq \mu N = \mu(mg - ma \sin \theta)$$

$$\mu \geq \frac{a \cos \theta}{g - a \sin \theta}$$

**67. (A), (C)**

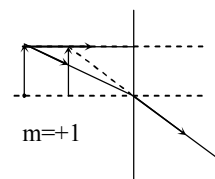
Apparent position of the object wrt lens.

$$u = \left( \frac{10}{1} + \frac{10}{2} \right) = 15 \text{ cm}$$

$$\frac{1}{15} + \frac{1}{v} = \frac{2(1.5) - 1}{R}$$

$$v = 7.5 \text{ cm}$$

$$\text{Image size} = \frac{7.5}{15} \times 1 = 0.5 \text{ cm}$$

**68. (A) (B) and (C)**

$$\frac{1}{f} = (1.5 - 1) \left( \frac{1}{10} - \frac{1}{50} \right), f = 25 \text{ cm}$$

$$-\frac{1}{F} = \frac{2}{f} + \frac{1}{f_m} = \frac{2}{25} + \frac{1}{-25}, F = -25$$

**69. (B) and (C)**

The ray is intersecting  $y = 0$  line at  $x = 1$

and  $x = 40$  line at  $y = -1$ .

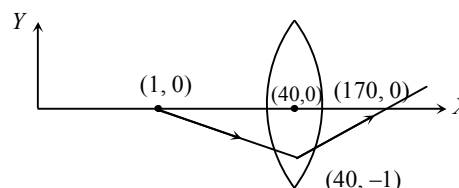
$$\therefore u = 39 \text{ cm}$$

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f} \Rightarrow v = 130 \text{ cm}$$

$\therefore$  Equation of refracted ray is

$$130y = x - 170$$

If space on the right of the lens is filled with liquid of  $\mu = 4/3$ , then



$$\frac{1.5}{v_1} + \frac{1}{39} = \frac{0.5}{30}$$

$$\frac{4}{3v} - \frac{1.5}{v_1} = \frac{\left(\frac{4}{3} - 1.5\right)}{-30}$$

$$v = -390 \text{ cm}$$

∴ Equation of refracted ray is  $390y + x + 330 = 0$

70. (D)

71. (A)

72. (C)

$$f_1 = f \text{ for no rotation of bottom cylinder} \quad \dots(i)$$

FBD of top cylinder :

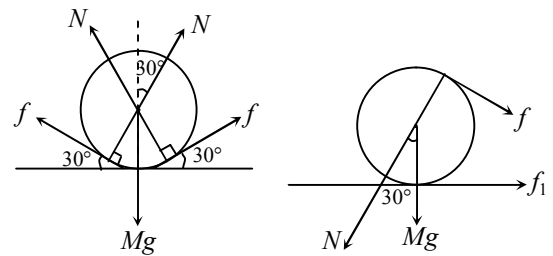
$$2N \cos 30 + 2f \sin 30 = Mg \quad \dots(ii)$$

FBD of bottom cylinder (left one)

$$N \sin 30 = f_1 + f \cos 30 \quad \dots(iii)$$

Solving (i), (ii) and (iii)

$$N = \frac{Mg}{2} \quad f = \frac{Mg}{2(2 + \sqrt{3})}$$



73. (A)

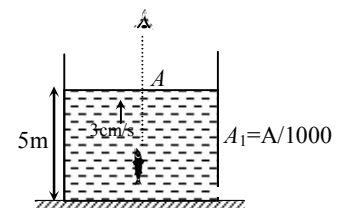
$$\text{Velocity of efflux } v = \sqrt{2g \times 5} = 10 \text{ m/s}$$

$$\text{Velocity of surface} = \frac{10 \times A/1000}{A} = 1 \text{ cm/s}$$

74. (A)

$$\text{Velocity of fish w.r.t surface in air} = \frac{3+1}{\mu} = 3 \text{ cm/s}$$

$$\text{Velocity as viewed directly by the observer} = 3 - 1 = 2 \text{ cm/s}$$





75. (3)

Let  $M_1$  be the mass of the rod.

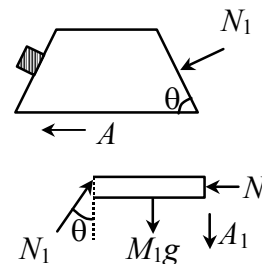
$$M_1 g - N_1 \cos \theta = M_1 A_1 \quad \dots (i)$$

$$N_1 \sin \theta = (M + M)A \quad \dots (ii)$$

$$A = g \tan \theta \quad \dots (iii)$$

relation between  $A_1$  and  $A$ 

$$A_1 = A \tan \theta$$

So by solving these equations  $M_1 = 3M$ 

76. (7)

77. (3)

78. (5)

79. (4)

80. (7)

81. (5)

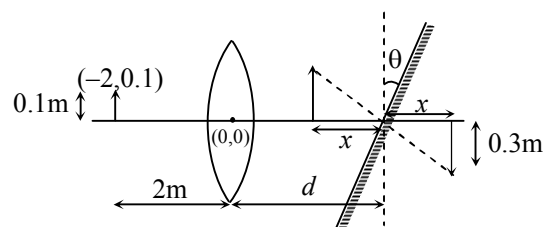
$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} - \frac{1}{-2} = \frac{1}{1.5}; \quad v = 6\text{m}$$

$$m = \frac{v}{u} = -3$$

$$x = 6 - d; \quad \tan \theta = \frac{0.3}{x}$$

$$\Rightarrow d = 5\text{m}.$$



82. (4)

Let the curved surface form the image of the object at a distance  $v_1$ , which acts as an object for second surface and final image is formed at a distance  $v$  from lens,

$$\therefore \frac{\mu_2}{v_1} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R} \quad \dots (1)$$

$$\frac{\mu_3}{v} - \frac{\mu_2}{v_1} = \frac{\mu_3 - \mu_2}{\infty} = 0 \quad \dots (2)$$

$$\text{Adding (1) \& (2)} \quad \frac{\mu_3}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R} = \frac{1}{2R}$$

$$u = -3R, v = 8R$$

$$\therefore \frac{\mu_3}{8R} + \frac{1}{3R} = \frac{1}{2R}$$

$$\therefore \mu_3 = 4/3$$

83. (2)

$$\vec{V}_{\text{obj, mirror}} = 4\hat{i} + 9\hat{j}$$

$$\frac{dx}{dt} = 4, \frac{dy}{dt} = 9$$

$$u = -x$$

$$-\frac{1}{10} = \frac{1}{V} + \frac{1}{-x}$$

$$V = \frac{-10x}{x-10}$$

$$V_{1x} = \frac{dV}{dt} = \left(\frac{10}{x-10}\right)^2 \left(\frac{dx}{dt}\right)$$

$$V_{1x} = -16$$

$$m = -\frac{V}{-x} = \frac{-10}{x-10} = \frac{y_1^0}{y}$$

$$V_{1y} = -\left(\frac{10}{x-10}\right) \frac{dy}{dt}$$

$$V_{1y} = -18$$

$$\vec{V}_{\text{image, mirror}} = -16\hat{i} - 18\hat{j}$$

$$\vec{V}_{\text{image}} = -12\hat{i} - 16\hat{j}$$

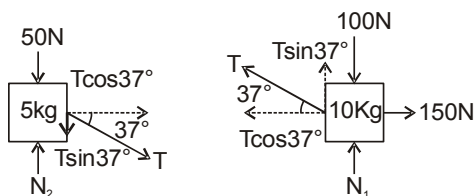
$$|V| = 20 \text{ cm/s}$$

$$\therefore z = 10 \text{ cm/s}$$

84. (2)

$$a = 10\text{ms}^{-2}$$

$$150 - T\cos 37^\circ = 10a$$



$$\therefore T = \frac{125}{2} \text{ N}$$