

SOLUTIONS

PHASE TEST-2

GZRA-1901, GZR-1901(A)

GZRS-1901

JEE MAIN PATTERN

Test Date: 15-10-2017



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PHYSICS

$$1. \quad \frac{\Delta T}{T} \times 100 = \frac{1}{25} \times 100 = 0.8\%$$

\therefore (B)

$$2. \quad ML^2T^{-2} = \frac{\alpha[L]^{1/2}}{[L]}$$

$$\alpha = [M][L^{5/2}][T^{-2}]$$

\therefore (D)

$$3. \quad \rho = 1 \text{ mm}, N = 100$$

$$\text{Least count, } C = \frac{P}{N} = \frac{1 \text{ mm}}{100} = 0.01 \text{ mm}$$

The instrument has a positive zero error $e = +NC = +4 \times 0.01 = +0.04 \text{ mm}$

Main scale reading is $2 \times (1 \text{ mm}) = 2 \text{ mm}$

Circular scale reading is $67 (0.01) = 0.67 \text{ mm}$

\therefore observed reading is $R_0 = 2 + 0.67 = 2.67 \text{ mm}$

So true reading = $R_0 - e = 2.63 \text{ mm}$

\therefore (C)

$$4. \quad \vec{r} = (2t - 3t^2)\hat{i} + 2t\hat{j} - t^2\hat{k}, \quad \vec{v} = (2 - 6t)\hat{i} + 2\hat{j} - 2t\hat{k}, \quad \vec{a} = -6\hat{i} - 2\hat{k}$$

$$\text{If } \vec{v} \perp \vec{a}, \quad \vec{v} \cdot \vec{a} = 0 \quad \therefore -6(2 - 6t) + 4t = 0, \quad 40t = 12$$

$$t = \frac{3}{10} = 0.3 \text{ s}$$

\therefore (C)

$$5. \quad \text{The maximum distance covered by the vehicle before coming to rest} = \frac{v^2}{2a} = \frac{(15)^2}{2 \times 0.3} = 375 \text{ m.}$$

$$\text{The corresponding time} = t = \frac{v}{a} = \frac{15}{0.3} = 50 \text{ sec.}$$

Therefore after 50 sec, the distance covered by the vehicle = 375 m, from the instant of beginning of braking.

The distance of the vehicle from the traffic signal after one minute = $(400 - 375) \text{ m} = 25 \text{ m}$.

\therefore (A)

$$6. \quad R = \frac{u^2}{g} \sin 2\theta = \frac{u^2}{g}$$

$$\text{Velocity of take off at } P \quad \text{or} \quad u = \sqrt{Rg} = \sqrt{90 \times 10} = 30 \text{ m/s}$$

$$v = \sqrt{u^2 + 2g \sin \theta S} \quad [v \rightarrow \text{velocity at point } O]$$

$$= \sqrt{(30)^2 + 2 \times 10 \times \frac{1}{\sqrt{2}} \times 80\sqrt{2}} = 50 \text{ m/s}$$

∴ (C)

7. If u is the initial speed of the second stone, then

$$0 = u^2 - 2g(4h)$$

$$\text{or} \quad u = \sqrt{8gh}$$

If they meet at the height x from ground,

$$\text{For A, } h - x = \frac{1}{2}gt^2$$

$$\text{For B, } x = (\sqrt{8gh})t - \frac{1}{2}gt^2$$

$$\therefore h = \sqrt{8gh}t$$

$$\text{or} \quad t = \sqrt{\frac{h}{8g}}$$

∴ (B)

8. As $F_1 - F_2 < 2\mu Mg$, so system will not accelerate. Again here $F_1 > F_2$, so block A is the driving block and block B is driven block. So friction on block A acts towards left but in the block B it may act left or right.

∴ (B)

9. Distance travelled along OE in $2s = 4 \times 2 = 8 \text{ m}$

$$\text{Distance travelled perpendicular to } OE \text{ in } 2s = \frac{1}{2}at^2 = \frac{1}{2}\left(\frac{6}{2}\right)^2 = 6 \text{ m}$$

$$\text{Displacement} = \sqrt{6^2 + 8^2} = 10 \text{ m}$$

∴ (D)

10. Normal \leq contact force $\leq \sqrt{(\text{normal})^2 + (\text{maximum friction})^2}$

$$Mg \leq F \leq \sqrt{(Mg)^2 + (\mu Mg)^2}$$

\therefore (C)

11. (D)

$f = \mu R = \mu mg$, where m is mass of the combination, $f = 0.5 \times 10 \times 10 \text{ N} = 50 \text{ N}$.

So, a force of 10 N is unable to start the motion of the system. There is no relative motion between A and B.

12. (A)

Given that $(\vec{F}_1 + \vec{F}_2) \cdot \vec{F}_1 = 0$

where $F_1 < F_2$

$$\therefore F_1^2 + F_1 F_2 \cos \theta = 0$$

Given that $F_2 = 2F_1$

$$F_1^2 + 2F_1^2 \cos \theta = 0$$

$$\cos \theta = -\frac{1}{2}$$

$$\therefore \theta = 2\pi/3$$

13. (D)

From the property of vector product, $\vec{A} \times \vec{B}$ is perpendicular to both \vec{A} and \vec{B} and $(\vec{A} + \vec{B})$ vector also, must lie in the plane formed by vector \vec{A} and \vec{B} . Thus \vec{C} must be perpendicular to $(\vec{A} + \vec{B})$ also but the cross product $(\vec{A} \times \vec{B})$ gives a vector \vec{C} which can not be perpendicular to itself. Thus the last statement is wrong.

14. (C)

15. (C)

Component of velocity in vertical should be same.

16. (D)

$$H = \frac{u_1^2 \sin^2 \theta_1}{2g} = \frac{u_2^2 \sin^2 \theta_2}{2g}$$

17. (B)

$$H = \frac{u^2 \cos^2 \beta}{2g} \Rightarrow 4\cos\beta = \sqrt{2gH}$$

$$t = \frac{u \cos \beta}{g} = \frac{\sqrt{2gH}}{g} \Rightarrow t = \sqrt{\frac{2H}{g}}$$

18. (D)

Since $v_{1Y} = v_{2Y} = 0$

And $Y_1 = Y_2 = -Y$

($a_{1Y} = a_{2Y} = -g \cos \theta$)

Hence from, $y = vt + \frac{1}{2}at^2$

Time taken for both the bullets will be same.

19. (A)

$$\vec{u} = i + 2\hat{j}$$

$$\therefore y = x \tan \theta - \frac{gx^2}{2u^2 \cos^2 \theta}$$

$$\text{or } y = x \cdot \frac{u_y}{u_x} - \frac{gx^2}{2 \cdot u_x^2}$$

$$\text{or } y = x \left(\frac{2}{1} \right) - \frac{gx^2}{2 \cdot (1)^2} \therefore y = 2x - 5x^2$$

20. (A)

Acceleration of m will give spring force. Then f.b.d. of M will give its acceleration.

21. (C)

Acceleration of A and B can be obtain by f.b.d. Then use kinematical equation.

22. (A)

23. (B)

24. (A)

25. (B)

26. (D)

27. Acceleration during ascent (a_1) = $g - \frac{F}{m}$ (downward)

Acceleration during descent (a_2) = $g + \frac{F}{m}$ (downward)

$$a_1 < a_2$$

$$\therefore t_1 > t_2$$

\therefore (B)

$$28. \quad f_1 = \mu_s m_1 g = 25\text{N}, \quad (a_2)_{\max} = \frac{f_1}{m_2} = \frac{5}{6} \text{ms}^{-2}$$

$$a_{\text{combined}} = \frac{F}{m_1 + m_2} = 1\text{ms}^{-2}$$

$(a_2)_{\max} < a_{\text{combined}}$, \therefore there will be slipping between the blocks.

$$\therefore f = \mu_k m_1 g = 12\text{N}$$

$$a_2 = \frac{f}{m_2} = \frac{12}{30} = 0.4 \text{ms}^{-2}$$

\therefore (B)

29. For safe crossing, the condition is that the man must cross the road by the time the truck covers the distance $4 + AC$ or $4 + 2\cot\theta$

$$\therefore \frac{4 + 2\cot\theta}{8} = \frac{2/\sin\theta}{v}$$

$$\text{or } v = \frac{8}{2\sin\theta + \cos\theta} \quad \dots(i)$$

$$\text{For minimum } v, \quad \frac{dv}{d\theta} = 0 \Rightarrow \tan\theta = 2$$

$$\text{From equation (i),} \quad v_{\min} = \frac{8}{\sqrt{5}} = 3.57 \text{ m/s}$$

\therefore (C)

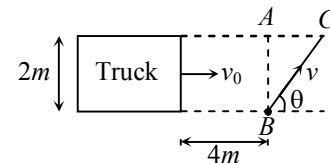
$$30. \quad \frac{1}{2}gt^2 = H \quad \dots(i)$$

$$gt = v_y \quad \dots(ii)$$

$$v_x = v_y$$

$$\text{Range} = u_x t = v_y t = gt^2 = 2H$$

\therefore (B)



CHEMISTRY

31. (D)

32. (B)

$$\text{K.E.} = \frac{3}{2} RT$$

$$\therefore (\text{K.E.})_1 = \frac{3}{2} \times R \times 400 \Rightarrow (\text{K.E.})_2 = \frac{3}{2} \times R \times 800$$

$$\therefore \frac{(\text{K.E.})_2}{(\text{K.E.})_1} = 2 \text{ or } (\text{K.E.})_2 = 2 (\text{K.E.})_1$$

33. (D)

34. (C)

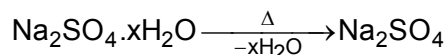
$$2\pi r = n\lambda$$

$$\text{or } \lambda = \frac{2\pi r}{n} = \frac{2\pi an^2}{n} \quad [z = 1 \text{ for H}]$$

$$\text{or } \lambda = 2\pi an = 4\pi a$$

35. (B)

36. (D)



Let the total molecular weight of the compound be y

$$\text{Then, } y - \frac{55.9}{100}y = 142 \quad [\because \text{M.W. of Na}_2\text{SO}_4 = 142]$$

$$\frac{44.1}{100}y = 142$$

$$y = \frac{142 \times 100}{44.1} = 321.99$$

Now, M.W. of $\text{Na}_2\text{SO}_4 \cdot x\text{H}_2\text{O} = 142 + 18x$

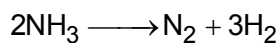
$$142 + 18x = 321.99$$

$$x = \frac{321.99 - 142}{18} = 10$$

37. (B)

$$\text{Molality} = \frac{\frac{20 \times 0.75}{60}}{\frac{50}{1000}} = 5$$

38. (C)



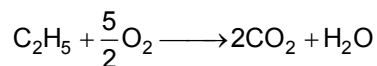
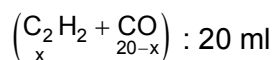
$$M_{\text{mix}} = \frac{17}{1 + \alpha}$$

$$\frac{r_{\text{mix}}}{r_{\text{SO}_2}} = 2 = \sqrt{\frac{64}{\frac{17}{1 + \alpha}}}$$

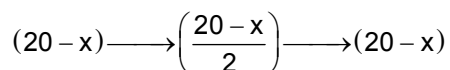
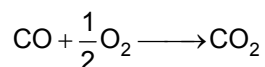
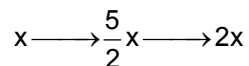
$$68 = 64 + 64\alpha \Rightarrow \alpha = \frac{1}{16}$$

$$\% \text{ dissociation} = 6.25\%$$

39. (A)



Initial :



Volume after reaction = 34 ml

$$V_{\text{CO}_2} \text{ formed} + V_{\text{O}_2} \text{ remained} = 34 \text{ ml}$$

$$2x + (20 - x) + \left\{ 30 - \left(\frac{5}{2}x + \frac{20 - x}{2} \right) \right\} = 34$$

$$20 + x + 30 - 2x - 10 = 34$$

$$40 - x = 34$$

$$x = 6 \text{ ml}$$

or

After passing KOH,

8 ml of O₂ remained

$$V_{\text{absorbed}} = 34 - 8 = 26$$

$$V_{\text{CO}_2} = 26$$

$$20 + x = 26$$

$$x = 6 \text{ ml}$$

40. (D)

$$\text{At } 27^\circ\text{C}; 1V = n_{\text{He}} R(300) \Rightarrow n_{\text{He}} = \frac{V}{300R}$$

$$\text{at } 127^\circ\text{C}; 2V = (n_{\text{He}} + n_{\text{P}})R(400) \Rightarrow n_{\text{He}} + n_{\text{P}} = \frac{V}{200R}$$

$$\therefore n_{\text{P}} = \frac{V}{600R}$$

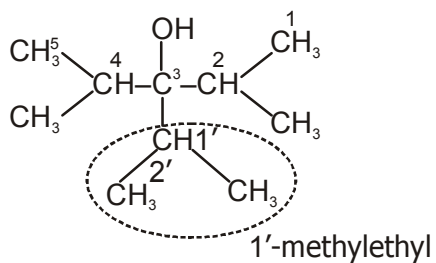
$$\text{at } 327^\circ\text{C}; PV = \left(\frac{V}{300R} + \frac{2V}{600R} \right) R(600)$$

$$P = 4 \text{ atm}$$

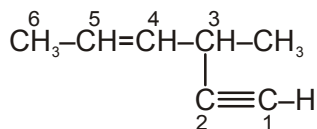
41. (B)

Those atoms which attached with sp hybridized carbon then it is present linearly.

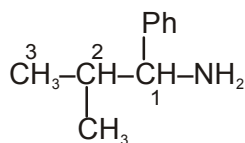
42. (A)



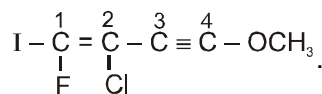
43. (C)



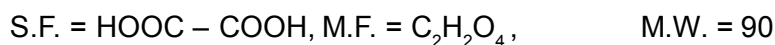
44. (B)



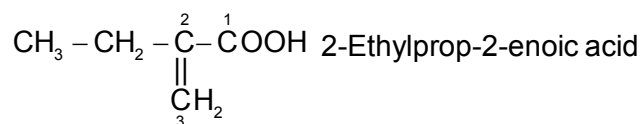
45. (D)



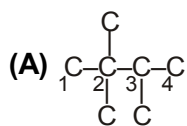
46. (C)



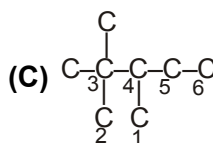
47. (B)



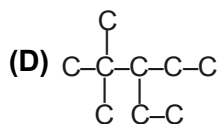
48. (B)



2, 2, 3-Trimethylbutane

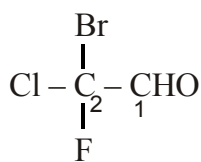


3, 3-Dimethylhexane

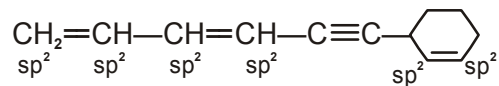


3-Ethyl-2,2-dimethyl pentane

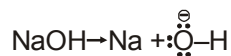
49. (A)



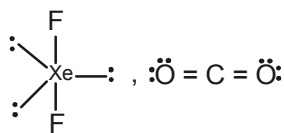
50. (A)



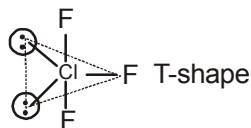
51. (B)



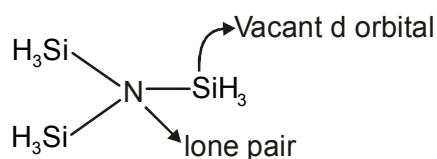
52. (B)



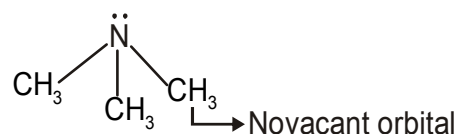
53. (D)



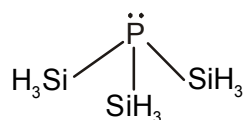
54. (B)



(due to Back Bonding)



(No back bonding)



(No back bonding due to large size of atoms)

55. (D)

As electronegativity of halogen attached with sulphur increases, sulphur becomes more electron deficient and hence its tendency of get electrons from oxygen through $p\pi - d\pi$ bonding also increases i.e. extent of $p\pi - d\pi$ bonding increases and hence, bond order also increases.

56. (A)

(A) Lattice energy depend upon :

- (i) Size of cation and anion both
- (ii) Product of charges at cation & anion

(B) $\text{CdCl}_2 > \text{CaCl}_2$ – Both Hydration & Lattice is high than CaCl_2

As per (born haber cycle)

(C) $\text{F}^- > \text{Cl}^- > \text{Br}^- > \text{I}^-$ (Hydration energy)

so, $\text{AgF} > \text{AgCl} > \text{AgBr} > \text{AgI}$ (Solubility in water)

(D) $\text{Be}_3\text{N}_2 > \text{Mg}_3\text{N}_2 > \text{Ca}_3\text{N}_2$ (Thermal stability)

$$\frac{a_1 + \left(\frac{p-1}{2}\right)d}{a_1 + \left(\frac{q-1}{2}\right)d} = \frac{p}{q} \quad (i)$$

for a_6 put $\frac{p-1}{2} = 5$ and for a_{21} put $\frac{p-1}{2} = 20$

$$\Rightarrow p = 11, q = 41$$

$$\Rightarrow \frac{p}{q} = \frac{11}{41}$$

63. (D)

$$\frac{C_1P}{C_2P} = \frac{2}{1}$$

$\therefore C_2$ is the midpoint of C_1 and P

$$\therefore P(8, 0)$$

equation of line through P

$$y - 0 = m(x - 8)$$

$$mx - y - 8m = 0$$

perpendicular from $(2, 0) =$ radius i.e. 2

$$\left| \frac{2m - 8m}{\sqrt{1 + m^2}} \right| = 2 \quad \Rightarrow \quad 9m^2 = 1 + m^2 \quad \Rightarrow \quad m = -\frac{1}{2\sqrt{2}} \text{ or } \frac{1}{2\sqrt{2}} \text{ (rejected)}$$

$$\therefore y = -\frac{1}{2\sqrt{2}}(x - 8)$$

for y-intercept put $x = 0$

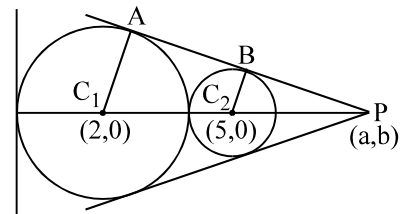
$$y = \frac{8}{2\sqrt{2}} = 2\sqrt{2}$$

64. (A)

Let equation of line $\frac{x}{\cos \theta} = \frac{y}{\sin \theta} = r$

$(OA \cos \theta, OA \sin \theta)$, and $(OB \cos \theta, OB \sin \theta)$

Will satisfy $y - x - 10 = 0$ and $y - x - 20 = 0$



respectively

$$\text{If } P(r \cos \theta, r \sin \theta) \text{ then } \frac{1}{r^2} = \left(\frac{\sin \theta - \cos \theta}{10} \right)^2 + \left(\frac{\sin \theta - \cos \theta}{20} \right)^2$$

$$\Rightarrow (r \cos \theta - r \sin \theta)^2 = 80 \Rightarrow \text{locus of } P \text{ is } (y - x)^2 = 80$$

65. (D)

Here $ax + by = 20$ is a chord with $(2, 3)$ as its mid-point.

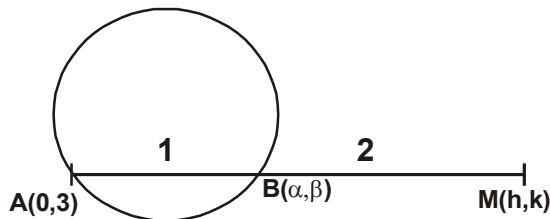
$$\Rightarrow -\frac{a}{b} = -1 \quad \Rightarrow a = b$$

$$\text{Now, } 2a + 3b = 20$$

$$\Rightarrow 5a = 20 \Rightarrow a = b = 4$$

$$\text{Hence } a^{103} + b^{103} = 2^{207}$$

66. (D)



$$\alpha = \frac{h}{3} \quad \beta = \frac{k+6}{3}$$

$$\text{Hence } \frac{h^2}{9} + \frac{(k+6)^2}{9} + 4 \times \frac{h}{3} - 6 \times \frac{k+6}{3} + 9 = 0 \Rightarrow h^2 + k^2 + 12h - 6k + 9 = 0$$

$$\Rightarrow x^2 + y^2 + 12x - 6y + 9 = 0$$

67. (A)

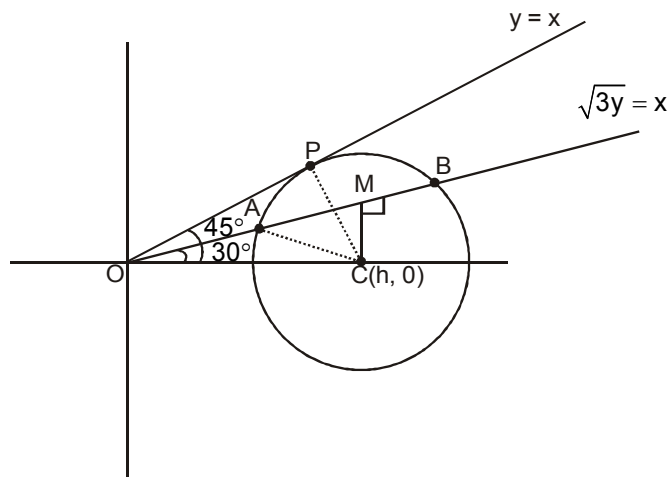
$$OP = CP = \frac{h}{\sqrt{2}} = AC$$

$$CM = h \sin 30^\circ = \frac{h}{2}$$

From $\triangle ACM$

$$AC^2 = CM^2 + AM^2$$

$$\frac{h^2}{2} = 1 + \frac{h^2}{4} \Rightarrow h^2 = 4$$



$$h = 2$$

$$\text{radius} = \frac{h}{\sqrt{2}} = \sqrt{2}$$

equation of circle

$$(x-2)^2 + y^2 = 2$$

68. (C)

$$a, ar, ar^2, ar^3 \quad (\text{G.P.})$$

$$a - 2, ar - 7, ar^2 - 9, ar^3 - 5 \quad (\text{A.P.})$$

$$\therefore 2(ar - 7) = (a - 2) + (ar^2 - 9)$$

$$\Rightarrow 2ar - 14 = a(1 + r^2) - 11$$

$$\Rightarrow a(1 - r)(r - 1) = 3 \quad \dots\dots(i)$$

$$\text{Also } 2(ar^2 - 9) = (ar - 7) + (ar^3 - 5)$$

$$\Rightarrow 2ar^2 - 18 = ar(1 + r^2) - 12$$

$$\Rightarrow a.r(r - 1)(1 - r) = 6 \quad \dots\dots(ii)$$

From (i) & (ii), $r = 2$ and $a = -3$

$$\therefore \text{third term of A. P.} = ar^2 - 9 = (-3).(2)^2 - 9 = -12 - 9 = -21$$

69. (B)

A.M \geq G.M

$$\frac{a+b+c}{3} \geq (abc)^{\frac{1}{3}}; \text{ for } (a, b, c > 0)$$

$$\Rightarrow a + b + c \geq 3(abc)^{\frac{1}{3}}$$

but given $ab^2c^3, a^2b^3c^4, a^3b^4c^5$ are in A.P

$$\text{Hence } 2abc = 1 + a^2b^2c^2 \Rightarrow (abc - 1)^2 = 0 \Rightarrow abc = 1$$

hence minimum value of

$$a + b + c = 3(abc)^{\frac{1}{3}} = 3.(1)^{\frac{1}{3}} = 3$$

70. (C)

Let T_r be the r^{th} term of given series, $T_r = \frac{2r+1}{r(r+1)(2r+1)} = \frac{6}{r(r+1)} = 6 \left[\frac{1}{r} - \frac{1}{r+1} \right]$

$$\sum_{r=1}^{35} T_r = 6 \left[1 - \frac{1}{2} + \frac{1}{2} - \frac{1}{3} + \dots + \frac{1}{35} - \frac{1}{36} \right] = 6 \left[1 - \frac{1}{36} \right] = \frac{35}{6}$$

71. (C)

$$S = \frac{5}{13} + \frac{55}{13^2} + \frac{555}{13^3} + \dots \quad \text{---(i)}$$

$$\frac{S}{13} = \frac{5}{13^2} + \frac{55}{13^3} + \dots \infty \quad \text{---(ii)}$$

(i) - (ii)

$$\frac{12}{13}S = \frac{5}{13} + \frac{50}{13^2} + \frac{500}{13^3} + \dots \Rightarrow S = \frac{13}{12} \times \left[\frac{\frac{5}{13}}{1 - \frac{10}{13}} \right] = \frac{65}{36}$$

72. (A)

$$\frac{x}{-\frac{1}{\lambda}} + \frac{y}{+1} = 1 \quad \frac{x}{-3} + \frac{y}{\frac{3}{2}} = 1$$

$$\left| \left(-\frac{1}{\lambda} \right) \right| |(-3)| = 1 \cdot \frac{3}{2}$$

 $\lambda = 2$ (Here λ can't be negative)

73. (C)

$$P \equiv \frac{x}{\cos \frac{\pi}{4}} = \frac{y}{\sin \frac{\pi}{4}} = 6\sqrt{2} \Rightarrow x = 6, y = 6$$

Since $P(6,6)$ lie on circle

$$72 + 12(g+f) + c = 0 \quad \text{.....(i)}$$

Since $y = x$ touches the circle, then

$$2x^2 + 2x(g+f) + c = 0 \text{ has equal roots } D = 0$$

$$4(g + f)^2 = 8c \Rightarrow (g + f)^2 = 2c \quad \dots\dots(ii)$$

From equation (i), we get

$$(12(g + f))^2 = [-(c + 72)]^2 \Rightarrow 144(2c) = (c + 72)^2 \Rightarrow (c - 72)^2 = 0 \Rightarrow c = 72$$

74. (B)

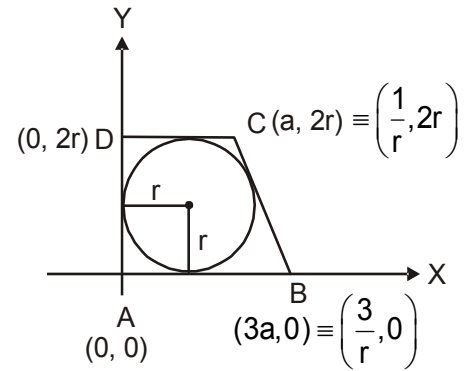
$$\text{Area of trapezium ABCD} = \frac{1}{2}(a + 3a)(2r) = 4 \Rightarrow ar = 1$$

$$\text{Equation of line BC is } y = -r^2\left(x - \frac{3}{r}\right)$$

$$\text{or, } y + r^2x - 3r = 0$$

\therefore BC is the tangent to the circle

$$\Rightarrow \frac{|r + r^3 - 3r|}{\sqrt{1+r^4}} = r \Rightarrow r^4 + 4 - 4r^2 = 1 + r^4 \Rightarrow r = \frac{\sqrt{3}}{2}$$



75. (C)

76. (A)

77. (C)

$$\left. \begin{array}{l} _ _ 20 \\ _ _ 40 \\ _ _ 60 \\ _ _ 04 \end{array} \right\} \begin{array}{l} 3 \times 4 = 24 \end{array} \qquad \left. \begin{array}{l} _ _ 12 \\ _ _ 16 \\ _ _ 24 \\ _ _ 64 \end{array} \right\} \begin{array}{l} 2 \times 2 \times 4 = 16 \end{array}$$

Total number of numbers = 24+16= 40

78. (A)

Alphabetical order of letters is B, E, K, R, U

words with 'B' = 4! = 24

words with 'E' = 4! = 24

words with 'KB' = 3! = 6

Words with 'KE' = 3! = 6

Words with 'KR' = 3! = 6

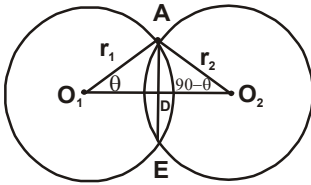
Next word will be KUBER

Whose rank is = 24 + 24 + 18 + 1 = 67

79. (A)

The circumcentre of ΔPQR will be orthocentre of ΔABC which is at (1, 1).

80. (A)



Let O_1 and O_2 are the centre of circles with radii r_1 and r_2 respectively and $\angle AO_1O_2 = \theta$

$$AD = r_1 \sin \theta; AD = r_2 \cos \theta$$

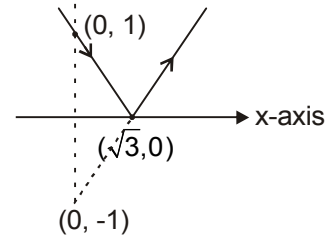
$$AD^2 \left(\frac{1}{r_1^2} + \frac{1}{r_2^2} \right) = 1 \Rightarrow AD = \frac{r_1 r_2}{\sqrt{r_1^2 + r_2^2}} \text{ so } AE = 2AD$$

81. (A)

$$x + \sqrt{3}y = \sqrt{3}$$

$$(y+1) = \frac{1}{\sqrt{3}}x$$

$$\sqrt{3}y = x - \sqrt{3}$$



82. (A)

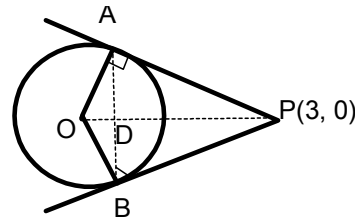
$$\text{Equation of AB is } T = 0 \text{ i.e. } x = \frac{4}{3}, OD = \frac{4}{3}$$

$$\Rightarrow AD^2 = OA^2 - OD^2$$

$$\Rightarrow AD^2 = 4 - \frac{16}{9} = \frac{20}{9}$$

$$\Rightarrow AD^2 = \frac{2\sqrt{5}}{3} \Rightarrow AB = \frac{4\sqrt{5}}{3} \Rightarrow \text{Area of triangle}$$

$$PAB = \frac{1}{2} \cdot \frac{4\sqrt{5}}{3} \cdot \left(3 - \frac{4}{3} \right) = \frac{10\sqrt{5}}{9} \text{ sq. units}$$



83. (B)

Let $y = m_1x$ and $y = m_2x$ be the two lines represented by $ax^2 + 2hxy + by^2 = 0$ so that

$$m_1 + m_2 = -\frac{2h}{b} \text{ and } m_1 m_2 = \frac{a}{b} \quad \dots(1)$$

Given $m_2 = m_1^2$

$$\therefore \text{From (1), } m_1 + m_1^2 = -\frac{2h}{b} \quad \dots(2)$$

$$\text{and } m_1 m_1^2 = \frac{a}{b} \text{ i.e., } m_1^3 = \frac{a}{b} \quad \dots(3)$$

The required condition is obtained by eliminating m_1 between (2) and (3).

$$\text{Cubing (2), we get } (m_1 + m_1^2)^3 = \left(-\frac{2h}{b}\right)^3$$

$$\Rightarrow m_1^3 + m_1^6 + 3m_1^3(m_1 + m_1^2) = -\frac{8h^2}{b^3}$$

$$\Rightarrow \frac{a}{b} + \frac{a^2}{b^2} + 3\frac{a}{b}\left(-\frac{2h}{b}\right) = -\frac{8h^3}{b^3} \quad [\text{Using (2) and (3)}]$$

$$\Rightarrow ab^2 + a^2b - 6abh = -8h^3 \quad \text{or } ab(a + b) - 6abh + 8h^3 = 0.$$

84. (B)

The equation of the bisectors of the angles between the lines $x^2 - 2pxy - y^2 = 0$ is

$$\frac{x^2 - y^2}{1 - (-1)} = \frac{xy}{-p} \quad \text{or} \quad \frac{x^2 - y^2}{2} = -\frac{xy}{p}$$

$$\text{i.e. } x^2 + \frac{2}{p}xy - y^2 = 0 \quad \dots(1)$$

$$\text{Also, } x^2 - 2qxy - y^2 = 0 \quad \dots(2)$$

is the equation of the bisectors of the angles between the same lines (given).

$$\text{From (1) and (2), by comparing coefficients, we get } \frac{1}{1} = \frac{2/p}{-2q} = \frac{-1}{-1}$$

$$\text{i.e. } 1 = -\frac{1}{pq} \quad \text{or } pq = -1.$$

85. (A)

86. (C)

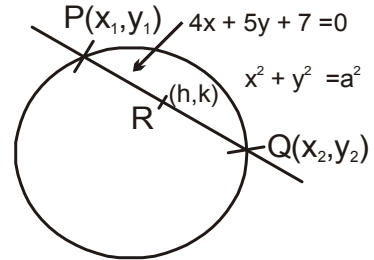
$$h = \frac{x_1 + x_2}{2}, k = \frac{y_1 + y_2}{2}$$

$$x^2 + \left(\frac{4x+7}{-5}\right)^2 = a^2$$

$$\Rightarrow 41x^2 + 56x + 49 - a^2 \cdot 25 = 0$$

$$\therefore \frac{x_1 + x_2}{2} = \frac{-56}{41 \times 2} = \frac{-28}{41}$$

$$\text{Similarly, } \frac{y_1 + y_2}{2} = \frac{-70}{41 \times 2} = \frac{-35}{41}$$



87. (B)

If θ be the angle that the line $x - 2y - 1 = 0$ makes with the positive x -axis, measured in the

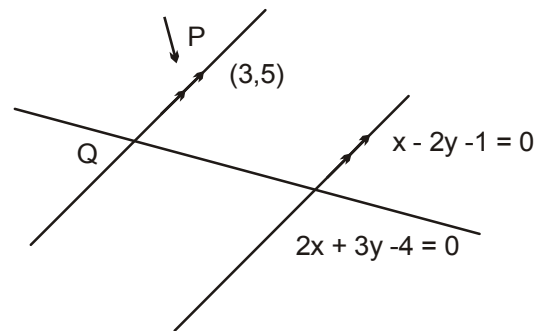
anti-clockwise sense, then $\tan \theta = \frac{1}{2} \quad \therefore \cos \theta = \frac{2}{\sqrt{5}}, \sin \theta = \frac{1}{\sqrt{5}}$

$$Q \equiv (3 + r \cos \theta, 5 + r \sin \theta)$$

$$\therefore 2 \left(3 + r \cdot \frac{2}{\sqrt{5}}\right) + 3 \left(5 + \frac{r}{\sqrt{5}}\right) - 4 = 0$$

$$\Rightarrow r = \frac{-17\sqrt{5}}{7}$$

$$\therefore \text{distance} = \frac{17\sqrt{5}}{7} \text{ unit}$$



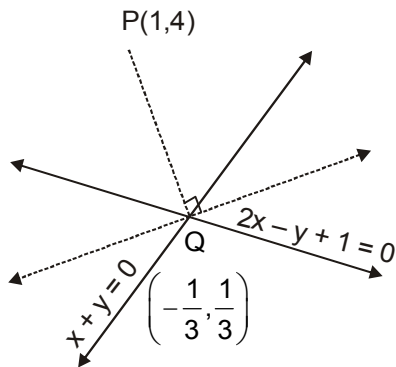
88. (C)

We have, $x + y + \lambda(2x - y + 1) = 0$

Clearly, it represents a family of line passing through the intersection of the lines $x + y = 0$ and $2x - y + 1 = 0$ i.e. the point $(-1/3, 1/3)$

The required line passes through $(-1/3, 1/3)$ and is perpendicular to the line joining $(1, 4)$ and $(-1/3, 1/3)$. So, its equation is

$$y - \frac{1}{3} = -\frac{4}{11}\left(x + \frac{1}{3}\right) \Rightarrow 12x + 33y = 7$$



89. (B)

The given circle $x^2 + y^2 - 4x - 6y - 12 = 0$ has its centre at $(2, 3)$ and radius equal to 5.

Let (h, k) be the coordinates of the centre of the required circle. Then, the point (h, k) divides the line joining $(-1, -1)$ to $(2, 3)$ in the ratio $3 : 2$, where 3 is the radius of the required circle. Thus, we have

$$h = \frac{3 \times 2 + 2(-1)}{3 + 2} = \frac{4}{5} \text{ and } k = \frac{3 \times 3 + 2(-1)}{3 + 2} = \frac{7}{5}$$

Hence, the equation of the required circle is

$$\left(x - \frac{4}{5}\right)^2 + \left(y - \frac{7}{5}\right)^2 = 3^2 \Rightarrow 5x^2 + 5y^2 - 8x - 14y - 32 = 0.$$

90. (A)

According to question

$A(0,0)$ and $B(1,1)$ are the end points of the diameter of the circle.